



basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

**ANNUAL NATIONAL ASSESSMENT
2014
GRADE 9 MATHEMATICS
EXEMPLAR QUESTIONS
MEMORANDUM**

KEY										
M	Method mark									
CA	Consistent Accuracy mark									
A	Accuracy mark									

1. MULTIPLE-CHOICE QUESTIONS

1.	1.1	C	1.2	C	1.3	B	1.4	C	1.5	B	Give 1 mark for each correct answer. [10]
	1.6	C	1.7	D	1.8	C	1.9	D	1.10	B	

2. NUMBERS, OPERATIONS AND RELATIONS

2.1.1	0,0067 ✓ A	1 mark	(1)
2.1.2	$3,56 \times 10^{-6}$ ✓ A	1 mark	(1)
2.1.3	$2,7, 2\sqrt{2}, 8$ ✓ A because $2\sqrt{2} \approx 2,83$.	1 mark	(1)
2.1.4	$-3\sqrt{3}, -5,25, -16$ ✓ A because $-3\sqrt{3} \approx -5,20$	1 mark	(1)
2.1.5	$9 < 13 < 16$ $3 < \sqrt{13} < 4$ ✓ A	Answer: 1 mark	(1)
2.2.1	$0,125 \div \sqrt{25}$ $= 0,125 \div 5$ ✓ M $= 0,025$ ✓ CA	5: 1 mark Answer: 1 mark	(2)
2.2.2	$\begin{aligned} &\left(2\frac{1}{2}\right)^2 + (0,5)^2 \\ &= \frac{25}{4} + 0,25 \text{ ✓ M} \\ &= \frac{25}{4} + \frac{1}{4} \text{ ✓ M} \\ &= \frac{26}{4} \\ &= 6\frac{1}{2} \text{ ✓ A} \end{aligned}$	$\frac{25}{4}$: 1 mark $\frac{1}{4}$: 1 mark Answer: 1 mark	(3)
	or		
	$6,25 + 0,25$ ✓ M $= 6,5$ ✓ ✓ A	6,25: 1 mark Answer: 2 marks	(3)
2.2.3	$\begin{aligned} &(\sqrt{169} + 3 \times 5) \div 2 \text{ ✓ M} \\ &= (13 + 15) \div 2 \text{ ✓ A} \\ &= 14 \text{ ✓ CA} \end{aligned}$	$(\sqrt{169} + 3 \times 5) \div 2$: 1 mark $13 + 15$: 1 mark Answer: 1 mark	(3)
2.2.4	$\begin{aligned} &\sqrt[3]{10^3} \times \sqrt{0,01} \\ &= 10 \times 0,1 \text{ ✓ ✓ M} \\ &= 1 \text{ ✓ CA} \end{aligned}$	10: 1 mark 0,1: 1 mark Answer: 1 mark	(3)

2.3	$96:120 \checkmark \mathbf{M}$ = 8:10 = 4:5 $\checkmark \mathbf{A}$	Ratio: 1 mark Answer: 1 mark	(2)
2.4	$\frac{250}{50} : \frac{150}{50} : \frac{100}{50} \checkmark \mathbf{M}$ = 5:3:2 $\checkmark \mathbf{A}$	Simplifying : 1 mark Answer: 1 mark	(2)
2.5	$\frac{5}{3} : \frac{8}{3} \checkmark \mathbf{M}$ = 5:8 $\checkmark \mathbf{A}$	$\frac{5}{3} \div \frac{8}{3}$: 1 mark Answer: 1 mark	(2)
2.6	5:3:4: 12 First mass = $\frac{5}{12} \times 240 \text{ g} = 100 \text{ g} \checkmark \mathbf{A}$ Second mass = $\frac{3}{12} \times 240 \text{ g} = 60 \text{ g} \checkmark \mathbf{A}$ Third mass = $\frac{4}{12} \times 240 \text{ g} = 80 \text{ g} \checkmark \mathbf{A}$ or Third mass = $240 \text{ g} - (100 \text{ g} + 60 \text{ g}) = 80 \text{ g} \checkmark \mathbf{CA}$	Answer: 1 mark each	(3)
2.7	Decreased amount = $\frac{2}{5} \times R1\,250 \checkmark \mathbf{M}$ = R500 $\checkmark \mathbf{A}$	$\frac{2}{5}$: 1 mark Answer: 1 mark	(2)
2.8	Increased number = $\frac{5}{2} \times 280 \checkmark \mathbf{M}$ = 700 $\checkmark \mathbf{A}$	$\frac{5}{2}$: 1 mark Answer: 1 mark	(2)
2.9	$P \cdot n \cdot i = SI \checkmark \mathbf{M}$ $3\,000(n)(0,8) = 960 \checkmark \mathbf{M}$ $n = 4 \checkmark \mathbf{A}$ or $A = P(1 + ni) \checkmark \mathbf{M}$ $3\,960 = 3\,000(1 + 0,08n) \checkmark \mathbf{M}$ $1,32 = 1 + 0,08n$ $0,32 = 0,08n$ $n = 4 \checkmark \mathbf{A}$	Formula/substitution: 2 marks Answer: 1 mark	(3)
2.10	$A = P(1 + i)^n \checkmark \mathbf{M}$ $A = R6\,500(1 + 0,075)^3 \checkmark \mathbf{M}$ $A = R8\,074,93 \checkmark \mathbf{A}$ Interest=A-P = R1 574,93 $\checkmark \mathbf{CA}$ or Year 1: $R6\,500 \times 7,5\% = R487,50 \checkmark \mathbf{M}$ Year 2: $R6\,987,50 \times 7,5\% = R524,06 \checkmark \mathbf{M}$ Year 3: $R7\,511,56 \times 7,5\% = R563,37 \checkmark \mathbf{M}$ Total interest is R1 574,93 $\checkmark \mathbf{M}$	Formula/substitution: 2 marks Calculation: 1 mark Answer: 1 mark	(4)
2.11	$A = P(1 + i)^n \checkmark \mathbf{M}$ $A = R10\,000(1 + 0,1)^3 \checkmark \checkmark \mathbf{M}$ = R13 310,00 $\checkmark \mathbf{A}$ or Year 1: $R10\,000 \times 10\% = R1\,000,00 \checkmark \mathbf{M}$ Year 2: $R11\,000 \times 10\% = R1\,100,00 \checkmark \mathbf{M}$ Year 3: $R12\,100 \times 10\% = R1\,210,00 \checkmark \mathbf{M}$ The amount = $R10\,000 + R3\,310,00$ = R13 310,00 $\checkmark \mathbf{CA}$	Formula/substitution: 3 marks Answer: 1 mark	(4)

<p>2.12</p> <table border="1" style="display: inline-table; vertical-align: middle;"> <tr><th style="text-align: center;">Speed (km/h)</th><th style="text-align: center;">Time (h)</th></tr> <tr><td style="text-align: center;">80</td><td style="text-align: center;">3</td></tr> <tr><td style="text-align: center;">50</td><td style="text-align: center;">x</td></tr> </table> <p>$50x = 80(3) \checkmark \checkmark \mathbf{M}$ (indirect proportion) $x = \frac{80(3)}{50} \checkmark \mathbf{A}$ $= 4,8 \text{ h} \checkmark \mathbf{CA}$</p> <p>or</p> <p>$s = \frac{d}{t}$ $d = 80 \frac{\text{km}}{\text{h}} \times 3 \text{ h}$ $d = 240 \text{ km} \checkmark \checkmark \mathbf{M}$ $t = \frac{d}{s}$ $t = \frac{240 \text{ km}}{50 \text{ km/h}}$ $= 4,8 \text{ hours or } 4 \text{ hours } 48 \text{ min} \checkmark \checkmark \mathbf{CA}$</p>	Speed (km/h)	Time (h)	80	3	50	x	<p>Formula/substitution: 2 marks x: 1 mark Answer: 1 mark</p>	<p>(4)</p>
Speed (km/h)	Time (h)							
80	3							
50	x							
<p>2.13</p> <table border="1" style="display: inline-table; vertical-align: middle;"> <tr><td style="text-align: center;">Length in m</td><td style="text-align: center;">3,5</td><td style="text-align: center;">x</td></tr> <tr><td style="text-align: center;">Shadow in m</td><td style="text-align: center;">5,2</td><td style="text-align: center;">29,2</td></tr> </table> <p>$\frac{x}{29,2} = \frac{3,5}{5,2} \checkmark \checkmark \mathbf{M}$ (direct proportion) $x = \frac{3,5 \times 29,2}{5,2} \checkmark \mathbf{M}$ $= 19,65 \text{ m} \checkmark \mathbf{A}$</p>	Length in m	3,5	x	Shadow in m	5,2	29,2	<p>Formula/substitution: 2 marks x: 1 mark Answer: 1 mark</p>	<p>(4)</p>
Length in m	3,5	x						
Shadow in m	5,2	29,2						

3. PATTERNS, FUNCTIONS AND ALGEBRA

<p>3.1.1</p> $(2x)^2 + 3x^2$ $= 4x^2 + 3x^2 \checkmark \mathbf{M}$ $= 7x^2 \checkmark \mathbf{CA}$	<p>$4x^2$: 1 mark Answer: 1 mark</p>	<p>(2)</p>
<p>3.1.2</p> $(a^2 b^3)^2 \cdot ab^2 - (ab)^5$ $= a^4 b^6 ab^2 - a^5 b^5 \checkmark \checkmark \mathbf{M}$ $= a^5 b^8 - a^5 b^5 \checkmark \mathbf{M}$ $= a^5 b^5 (b^3 - 1) \checkmark \mathbf{A}$	<p>$a^4 b^6 ab^2$: 1 mark $a^5 b^5$: 1 mark Applying exponential laws: 1 mark Answer: 1 mark</p>	<p>(4)</p>
<p>3.1.3</p> $\frac{5a^2 b}{3ab} \times \frac{27}{20a^3 b} \checkmark \mathbf{M}$ $= \frac{9}{4a^2 b} \checkmark \checkmark \mathbf{A}$	<p>Reciprocal: 1 mark 9: 1 mark $4a^2 b$: 1 mark</p>	<p>(3)</p>
<p>3.1.4</p> $\frac{2x^{-2} \times x^3}{2^2 x^2} \checkmark \mathbf{M}$ $= \frac{x}{2} \text{ or } \frac{1}{2} x \checkmark \mathbf{A}$	<p>Applying exponential laws: 1 mark Answer: 1 mark</p>	<p>(2)</p>
<p>3.1.5</p> $\frac{4x^{-2}}{(4x)^{-2}}$ $= \frac{4x^{-2}}{4^{-2} x^{-2}} \checkmark \mathbf{M}$ $= 4^3 \checkmark \mathbf{CA}$ $= 64 \checkmark \mathbf{A}$	<p>$4^{-2} x^{-2}$: 1 mark 4^3: 1 mark Answer: 1 mark</p>	<p>(3)</p>

3.1.6	$\begin{aligned} & \frac{x(x+2)}{x(x^2-2)} \times \frac{x-2}{(x+2)(x-2)} \checkmark \checkmark \checkmark \mathbf{M} \\ &= \frac{1}{x^2-2} \checkmark \mathbf{A} \end{aligned}$	$x(x + 2)$: 1 mark $x(x^2 - 2)$: 1 mark $(x + 2)(x - 2)$: 1 mark Answer: 1 mark	(4)
3.1.7	$\begin{aligned} & \frac{x-2}{2x} - \frac{x-3}{3x} \\ &= \frac{3(x-2) - 2(x-3)}{6x} \checkmark \checkmark \mathbf{M} \\ &= \frac{3x-6-2x+6}{6x} \checkmark \mathbf{M} \\ &= \frac{x}{6x} \checkmark \mathbf{A} \\ &= \frac{1}{6} \checkmark \mathbf{A} \end{aligned}$	Common denominator: 1 mark $3(x - 2) - 2(x - 3)$: 1 mark $3x - 6 - 2x + 6$: 1 mark Simplification: 1 mark Answer: 1 mark	(5)
3.1.8	$\begin{aligned} & 3a^{-2}b \times 24ab \\ &= \frac{9a^2b^{-2}}{3a^2b^{-2}} \checkmark \mathbf{M} \\ &= \frac{8b^4}{a^3} \checkmark \checkmark \mathbf{A} \end{aligned}$	Simplification: 1 mark $8b^4$: 1 mark a^3 : 1 mark	(3)
3.1.9	$\begin{aligned} & \frac{x^2 - 1}{3x + 3} \\ &= \frac{(x-1)(x+1)}{3(x+1)} \checkmark \checkmark \mathbf{M} \\ &= \frac{x-1}{3} \checkmark \mathbf{A} \end{aligned}$	$(x - 1)(x + 1)$: 1 mark $3(x + 1)$: 1 mark Answer: 1 mark	(3)
3.2.1	$\begin{aligned} & 3a^2bc^2(3a^2 - 4b - c) \\ &= 9a^4bc^2 \checkmark - 12a^2b^2c^2 \checkmark - 3a^2bc^3 \checkmark \mathbf{A} \end{aligned}$	1 mark for each term	(3)
3.2.2	$\begin{aligned} & (2x - 3)(x + 1) \\ &= 2x^2 \checkmark - x \checkmark - 3 \checkmark \mathbf{A} \end{aligned}$	$2x^2$: 1 mark $-x$: 1 mark -3 : 1 mark	(3)
3.2.3	$\begin{aligned} & (x - 3)^2 - x(x + 4) \\ &= x^2 - 6x + 9 - x^2 - 4x \checkmark \checkmark \mathbf{M} \\ &= -10x + 9 \checkmark \mathbf{A} \end{aligned}$	$x^2 - 6x + 9$: 1 mark $-x^2 - 4x$: 1 mark Answer: 1 mark	(3)
3.3.1	$\begin{aligned} & 10t^2 - 5t \\ &= 5t \checkmark (2t - 1) \checkmark \mathbf{A} \end{aligned}$	$5t$: 1 mark $2t - 1$: 1 mark	(2)
3.3.2	$\begin{aligned} & 81 - 100a^2 \\ &= (9 - 10a) \checkmark (9 + 10a) \checkmark \mathbf{A} \end{aligned}$	$9 - 10a$: 1 mark $9 + 10a$: 1 mark	(2)
3.3.3	$(x + y)(2 + a) \checkmark \checkmark \mathbf{A}$	Answer: 2 marks	(2)
3.3.4	$\begin{aligned} & 6x^3(a - b) + x(b - a) \\ &= 6x^3(a - b) - x(a - b) \checkmark \mathbf{M} \\ &= x(a - b)(6x^2 - 1) \checkmark \checkmark \checkmark \mathbf{A} \end{aligned}$	$-x(a - b)$: 1 mark x : 1 mark $(6x^2 - 1)$: 1 mark $(a - b)$: 1 mark	(4)
3.3.5	$\begin{aligned} & (a + b)(4 - x^2) \checkmark \checkmark \mathbf{M} \\ &= (a + b)(2 + x)(2 - x) \checkmark \mathbf{A} \end{aligned}$	Common factor: 1 mark $(4 - x^2)$: 1 mark $(2 + x)(2 - x)$: 1 mark	(3)
3.3.6	$\begin{aligned} & x^2 + 5x + 6 \\ &= (x + 3)(x + 2) \checkmark \checkmark \mathbf{M} \end{aligned}$	$(x + 3)$: 1 mark $(x + 2)$: 1 mark	(2)
3.3.7	$\begin{aligned} & 2a^2 - 18a + 36 \\ &= 2(a^2 - 9a + 18) \checkmark \mathbf{M} \\ &= 2(a - 6)(a - 3) \checkmark \checkmark \mathbf{A} \end{aligned}$	$2(a^2 - 9a + 18)$: 1 mark Answer: 2 marks	(3)

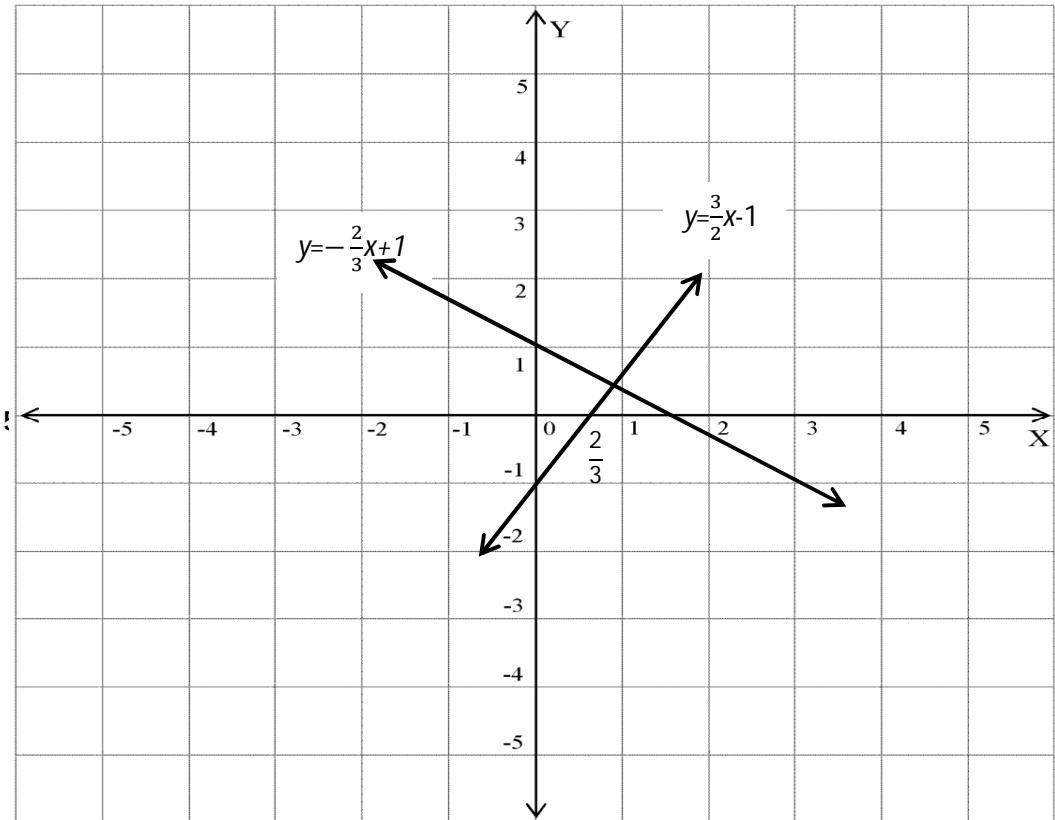
3.4.1	$2x - 5 = 5x + 16$ $-3x\checkmark = 21\checkmark \mathbf{M}$ or $-21\checkmark = 3x\checkmark \mathbf{M}$ $x = -7\checkmark \mathbf{A}$ $-7 = x\checkmark \mathbf{A}$	3x: 1 mark 21: 1 mark Answer: 1 mark (3)
3.4.2	$x - \frac{x-1}{2} = 3$ × 2: $2x - x + 1 = 6\checkmark \mathbf{M}$ $x + 1 = 6\checkmark \mathbf{M}$ $x = 5\checkmark \mathbf{A}$	Multiplying by 2: 1 mark Simplifying: 1 mark Answer: 1 mark (3)
3.4.3	$\frac{(x-2)}{4} + \frac{(2x+1)}{3} = \frac{5}{3}$ × 12: $3(x-2) + 4(2x+1) = 4 \times 5\checkmark \mathbf{M}$ $3x - 6 + 8x + 4 = 20\checkmark \mathbf{M}$ $11x = 22$ $x = 2\checkmark \mathbf{A}$	3(x-2): 1 mark 4(2x+1): 1 mark 4 × 5: 1 mark Simplifying: 1 mark Answer: 1 mark (5)
3.4.4	$(x-3)(x+4) = 0$ $x-3 = 0$ or $x+4 = 0$ $x = 3\checkmark$ or $x = -4\checkmark \mathbf{A}$	Answer: 2 marks (2)
3.4.5	$x^2 - 1 = 0$ $(x-1)(x+1) = 0\checkmark \mathbf{M}$ $x-1 = 0$ or $x+1 = 0$ $x = 1\checkmark$ or $x = -1\checkmark \mathbf{A}$ or $x^2 = 1\checkmark \mathbf{M}$ $\therefore x = 1\checkmark$ or $x = -1\checkmark \mathbf{A}$	Factorising: 1 mark Answer: 2 marks (3)
3.4.6	$3^{x+1} = 3^4\checkmark$ $x+1 = 4\checkmark$ $x = 3\checkmark$	Applying exponential law: 1 mark Equating exponents: 1 mark Answer: 1 mark (3)
3.4.7	$x^3 = -27$ $x = \sqrt[3]{-27}$ $x = -3\checkmark \mathbf{A}$	Answer: 2 marks (2)
3.4.8	$2^x = \frac{1}{64}$ $2^x = 2^{-6}\checkmark \mathbf{M}$ $x = -6\checkmark \mathbf{A}$	2^{-6} : 1 mark Answer: 1 mark (2)
3.5.1	$2x^3 - 3x^2 + 9x + 2$ $= 2(-2)^3 - 3(-2)^2 + 9(-2) + 2\checkmark \mathbf{M}$ $= -16 - 12 - 18 + 2\checkmark \mathbf{M}$ $= -44\checkmark \mathbf{A}$	Substitution: 1 mark Simplifying: 1 mark Answer: 1 mark (3)
3.5.2	$\frac{5ac}{b}$ $= \frac{5(2)(-\frac{1}{2})}{(-3)}\checkmark \mathbf{M}$ $= \frac{-5}{-3}\checkmark \mathbf{A}$	Substitution: 1 mark Simplifying: 2 marks (3)

	$= 1\frac{2}{3}$		
3.5.3	$3x^2 - 2xy - y^2$ $= 3(2)^2 - 2(2)(-3) - (-3)^2 \checkmark \mathbf{M}$ $= 12 + 12 - 9 \checkmark \mathbf{M}$ $= 15 \checkmark \mathbf{A}$	Substitution: 1 mark Simplifying: 2 marks Answer: 1 mark	(3)
3.5.4	$2 \times 3^{1-x}$ $= 2 \times 3^{1-(-2)}$ $= 2 \times 3^3 \checkmark \mathbf{M}$ $= 54 \checkmark \mathbf{A}$	Simplifying: 1 mark Answer: 1 mark	(2)

3.6.1	Figure	1	2	3	4	Answer: 2 marks	(2)										
	Number of black tiles	1	2	3	4												
	Number of white tiles	6	10	<u>14</u> $\checkmark \mathbf{A}$	<u>18</u> $\checkmark \mathbf{A}$												
3.6.2	$T_n = 4n + 2$					$4n$: 1 mark 2: 1 mark	(2)										
3.7.1	Triangular numbers $\checkmark \checkmark \mathbf{A}$					Answer: 2 marks	(2)										
3.7.2	$T_n = \frac{n(n+1)}{2} \checkmark \checkmark \mathbf{A}$ $T_{20} = \frac{20(20+1)}{2} \checkmark \mathbf{M}$ $= 210 \checkmark \mathbf{A}$					T_n : 2 marks Substitution: 1 mark Answer: 1 mark	(4)										
3.8.1	<table border="1"> <tr> <td>x</td> <td>-2</td> <td>-1</td> <td>0</td> <td>1</td> </tr> <tr> <td>y</td> <td>-11</td> <td>-8</td> <td>-5</td> <td>-2</td> </tr> </table>	x	-2	-1	0	1	y	-11	-8	-5	-2					1 mark each	(4)
x	-2	-1	0	1													
y	-11	-8	-5	-2													
3.8.2	<table border="1"> <tr> <td>x</td> <td>-3</td> <td>-1</td> <td>0</td> <td>1</td> </tr> <tr> <td>y</td> <td>1</td> <td>$-\frac{1}{3}$</td> <td>-1</td> <td>$-1\frac{2}{3}$ or $-\frac{5}{3}$</td> </tr> </table>	x	-3	-1	0	1	y	1	$-\frac{1}{3}$	-1	$-1\frac{2}{3}$ or $-\frac{5}{3}$					1 mark each	(4)
x	-3	-1	0	1													
y	1	$-\frac{1}{3}$	-1	$-1\frac{2}{3}$ or $-\frac{5}{3}$													

3.9.1	$x = 2 \checkmark \mathbf{A}$	Answer: 1 mark	(1)
3.9.2	$y = 2x \checkmark \checkmark \mathbf{A}$	Answer: 2 marks	(2)
3.9.3	$CE = 6 \text{ units} \checkmark \mathbf{A}$	Answer: 1 mark	(1)

3.10.1



X-intercept: 1 mark per graph ✓ + ✓ A

Y-intercept: 1 mark per graph ✓ + ✓ A

Correct labelling of graph: 1 mark per graph ✓ + ✓ A

(6)

3.10.2

The lines are perpendicular. ✓ A

(1)

3.11

 $P(3; 3)$ ✓

Answer: 2 marks

(2)

3.12.1

Gradient of $AD = \frac{4}{-2} = -2$.Equation of AD is $y = -2x + 4$ ✓ ✓-2x : 1 mark
4:1 markGradient of $BC = \frac{4}{-2} = -2$ Equation of BC is $y = -2x - 4$ ✓ ✓-2x : 1 mark
-4:1 mark

(4)

3.12.2

 $AD \parallel BC$ ✓ because the gradient of $AD =$ gradient of BC ✓ $AD \parallel BC$: 1 mark
Reason : 1 mark

(2)

4. SPACE AND SHAPE

4.1	Statement	Reason	
	$\hat{C}_1 = \hat{B}_2 + \hat{D}_1$ $75^\circ = x + 44^\circ \checkmark \mathbf{M}$ $\therefore x = 31^\circ \checkmark \mathbf{A}$	ext \angle of Δ = sum of int. opp \angle s $\checkmark \mathbf{A}$ or ext \angle of Δ	Statement: 1 mark Correct reason: 1 mark Answer for x : 1 mark Statement: 1 mark Correct reason: 1 mark
	$\hat{D}_2 = \hat{B}_2 = 31^\circ$ $\therefore y = 31^\circ \checkmark \mathbf{A}$	alt \angle s and $AD \parallel BC \checkmark \mathbf{A}$	(5)

4.2	Statement	Reason	
	<p>In $\triangle AEW$:</p> $\hat{E}_2 + \hat{W}_1 = 110^\circ \checkmark M$ <p>but $\hat{E}_2 = \hat{W}_1 = 55^\circ \checkmark M$</p> $\therefore x = \hat{E}_2 = 55^\circ \checkmark A$	<p>sum of \angles of $\Delta = 180^\circ \checkmark A$</p> <p>$\angle$s opp. equal sides of $\Delta \checkmark A$</p> <p>alt \angles and CS HW $\checkmark A$</p>	<p>Statement: 1 mark Correct reason: 1 mark Statement: 1 mark Correct reason: 1 mark Answer for x: 1 mark Correct reason: 1 mark</p>

4.3	Statement	Reason	
	$\hat{E} = 95^\circ - 30^\circ \checkmark M$ $= 65^\circ \checkmark A$ or $\hat{C}_1 = 180^\circ - 95^\circ$ $= 85^\circ \checkmark M/A$ $\hat{E} + 85^\circ + 30^\circ = 180^\circ$ $\hat{E} + 115^\circ = 180^\circ$ $\hat{E} = 65^\circ \checkmark A$	ext. \angle of $\triangle CED \checkmark A$ adj. suppl. \angle s or $B\hat{C}E$ is a str. \angle or \angle s on a str. line sum of \angle s of $\Delta = 180^\circ \checkmark A$	Statement: 1 mark Correct reason: 1 mark Answer: 1 mark
	$\hat{A} + \hat{E} = 180^\circ \checkmark M$ $\hat{A} = 115^\circ \checkmark A$	co - interior \angle s and $AB \parallel CD \checkmark A$	Statement: 1 mark Correct reason: 1 mark Answer: 1 mark

4.4	Statement	Reason	
	<p>In ΔABD and ΔCDB</p> $BD = BD \checkmark M$ $\hat{B}_2 = \hat{D}_1 = 90^\circ \checkmark M$ $AD = CB \checkmark M$ $\therefore \Delta ABD \equiv \Delta CDB \checkmark A$	<p>common ✓A</p> <p>given ✓A</p> <p>given ✓A</p> <p>$90^\circ H S \checkmark A$</p>	<p>Statement: 1 mark Correct reason:1 mark Statement: 1 mark Correct reason:1 mark Statement: 1 mark Correct reason:1 mark Statement: 1 mark Correct deduction:1 mark</p>

4.5.1	<table border="1"> <thead> <tr> <th>Statement</th><th>Reason</th></tr> </thead> <tbody> <tr> <td> $\hat{B}_1 + \hat{B}_2 + \hat{C}_1 + \hat{C}_2 = 180^\circ \checkmark M$ But $\hat{B}_1 = \hat{B}_2$ and $\hat{C}_1 = \hat{C}_2 \checkmark M$ $\therefore 2\hat{B}_1 + 2\hat{C}_1 = 180^\circ \checkmark A$ $\hat{B}_1 + \hat{C}_1 = 90^\circ \checkmark A$ $\therefore \hat{T}_2 = 90^\circ \checkmark A$ </td><td> co-int $\angle s$ and $AB \parallel DC \checkmark A$ given sum of $\angle s$ of $\Delta = 180^\circ \checkmark A$ sum of $\angle s$ of $\Delta = 180^\circ \checkmark A$ </td></tr> </tbody> </table>	Statement	Reason	$\hat{B}_1 + \hat{B}_2 + \hat{C}_1 + \hat{C}_2 = 180^\circ \checkmark M$ But $\hat{B}_1 = \hat{B}_2$ and $\hat{C}_1 = \hat{C}_2 \checkmark M$ $\therefore 2\hat{B}_1 + 2\hat{C}_1 = 180^\circ \checkmark A$ $\hat{B}_1 + \hat{C}_1 = 90^\circ \checkmark A$ $\therefore \hat{T}_2 = 90^\circ \checkmark A$	co-int $\angle s$ and $AB \parallel DC \checkmark A$ given sum of $\angle s$ of $\Delta = 180^\circ \checkmark A$ sum of $\angle s$ of $\Delta = 180^\circ \checkmark A$	Statement: 1 mark Correct reason: 1 mark Statement: 1 mark Correct reason: 1 mark Statement: 1 mark Correct reason: 1 mark Correct deduction: 1 mark Correct deduction: 1 mark (8)
Statement	Reason					
$\hat{B}_1 + \hat{B}_2 + \hat{C}_1 + \hat{C}_2 = 180^\circ \checkmark M$ But $\hat{B}_1 = \hat{B}_2$ and $\hat{C}_1 = \hat{C}_2 \checkmark M$ $\therefore 2\hat{B}_1 + 2\hat{C}_1 = 180^\circ \checkmark A$ $\hat{B}_1 + \hat{C}_1 = 90^\circ \checkmark A$ $\therefore \hat{T}_2 = 90^\circ \checkmark A$	co-int $\angle s$ and $AB \parallel DC \checkmark A$ given sum of $\angle s$ of $\Delta = 180^\circ \checkmark A$ sum of $\angle s$ of $\Delta = 180^\circ \checkmark A$					
<table border="1"> <thead> <tr> <th>Statement</th><th>Reason</th></tr> </thead> <tbody> <tr> <td> In ΔTCP and ΔBCT 1. $\hat{C}_2 = \hat{C}_1 \checkmark M$ 2. $\hat{P}_2 = \hat{T}_2 \checkmark M$ 3. $\hat{T}_1 = \hat{B}_1 \checkmark M$ $\therefore \Delta TCP \parallel \Delta BCT \checkmark M$ </td><td> given $\checkmark A$ both $90^\circ \checkmark A$ sum of $\angle s$ of $\Delta = 180^\circ \checkmark A$ $\angle \angle \angle \checkmark A$ </td></tr> </tbody> </table>		Statement	Reason	In ΔTCP and ΔBCT 1. $\hat{C}_2 = \hat{C}_1 \checkmark M$ 2. $\hat{P}_2 = \hat{T}_2 \checkmark M$ 3. $\hat{T}_1 = \hat{B}_1 \checkmark M$ $\therefore \Delta TCP \parallel \Delta BCT \checkmark M$	given $\checkmark A$ both $90^\circ \checkmark A$ sum of $\angle s$ of $\Delta = 180^\circ \checkmark A$ $\angle \angle \angle \checkmark A$	
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4.5.3	<table border="1"> <thead> <tr> <th>Statement</th><th>Reason</th></tr> </thead> <tbody> <tr> <td> $\frac{TC}{BC} = \frac{CP}{CT} = \frac{TP}{BT} \checkmark M$ $\frac{TC}{2TC} = \frac{4}{BT} \checkmark M$ $\frac{1}{2} = \frac{4}{BT} \checkmark A$ $\therefore BT = 8 \text{ cm} \checkmark A$ </td><td> prop. sides of similar $\Delta s \checkmark A$ $BC = 2TC \checkmark A$ </td></tr> </tbody> </table>	Statement	Reason	$\frac{TC}{BC} = \frac{CP}{CT} = \frac{TP}{BT} \checkmark M$ $\frac{TC}{2TC} = \frac{4}{BT} \checkmark M$ $\frac{1}{2} = \frac{4}{BT} \checkmark A$ $\therefore BT = 8 \text{ cm} \checkmark A$	prop. sides of similar $\Delta s \checkmark A$ $BC = 2TC \checkmark A$	Statement: 1 mark Correct reason: 1 mark Statement: 1 mark Correct reason: 1 mark Correct deduction: 1 mark Correct deduction: 1 mark (6)
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4.6.1	<table border="1"> <thead> <tr> <th>Statement</th><th>Reason</th></tr> </thead> <tbody> <tr> <td> In ΔABD and ΔACD $AB = AC \checkmark M$ $BD = CD \checkmark M$ $AD = AD \checkmark M$ $\therefore \Delta ABD \equiv \Delta ACD \checkmark A$ </td><td> given $\checkmark A$ given $\checkmark A$ common side $\checkmark A$ $s s s \checkmark A$ </td></tr> </tbody> </table>	Statement	Reason	In ΔABD and ΔACD $AB = AC \checkmark M$ $BD = CD \checkmark M$ $AD = AD \checkmark M$ $\therefore \Delta ABD \equiv \Delta ACD \checkmark A$	given $\checkmark A$ given $\checkmark A$ common side $\checkmark A$ $s s s \checkmark A$	Statement: 1 mark Correct reason: 1 mark Statement: 1 mark Correct reason: 1 mark Statement: 1 mark Correct reason: 1 mark Correct deduction: 1 mark Correct reason: 1 mark (8)
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4.6.2	$\hat{A}_1 = \hat{A}_2$ $\therefore DA \text{ bisects } BAC \checkmark$	(corr $\angle s$ of congruent Δs) \checkmark	(2)			

5. MEASUREMENT

5.1	<p>Let the length of the ladder be l.</p> $l^2 = 12^2 + 5^2 m^2 \quad (\text{Pyth}) \checkmark \checkmark \mathbf{M}$ $l^2 = 169 \text{ } m^2 \quad \checkmark \mathbf{A}$ $l = 13m \quad \checkmark \mathbf{A}$		<p>Formula/substitution: 2 marks Calculation: 1 mark Answer: 1 mark</p>	(4)
5.2.1	$PS^2 = AP^2 - AS^2$ $= (25 - 4) m^2 \checkmark \mathbf{M}$ $PS = 4,58 \text{ } m \checkmark \mathbf{A}$	Pyth $\checkmark \mathbf{A}$	<p>Formula/ substitution: 1 mark Reason: 1 mark Answer: 1 mark</p>	(3)
5.2.2	$PT = 3 \times AB = 12 \text{ } m \checkmark \mathbf{A}$		Answer: 1 mark	(1)
5.2.3	Kite.		Answer: 1 mark	(1)
5.2.4	<p>Area of the kite $= \frac{1}{2} \times PT \times AB \checkmark \mathbf{M}$ or $\frac{PT \times AB}{2}$</p> $= \frac{1}{2} \times 12 \text{ } m \times 4 \text{ } m \checkmark \mathbf{M}$ $= 24 \text{ } m^2 \checkmark \mathbf{A}$		<p>Formula: 1 mark Substitution: 1 mark Answer: 1 mark</p>	(3)
5.3.1	<p>Perimeter $= 2 \times 100 \text{ } m + 2\pi r$ $= 200 \text{ } m \checkmark + 2 \times 3,14 \times 30 \text{ } m \checkmark \mathbf{M}$ $\approx 388,4 \text{ } m \checkmark \mathbf{CA}$</p> <p>$\therefore$ the no. of rounds $= 4\ 000 \text{ } m \div 388,4 \text{ } m \checkmark \mathbf{M}$ $= 10,298661$</p> <p>Peter must run 11 times round the track. $\checkmark \mathbf{CA}$</p>		<p>Formula/ substitution: 2 marks Answer: 1 mark</p> <p>Calculation: 1 mark</p> <p>Answer: 1 mark</p>	(5)
5.3.2	<p>Area $= l \times b + \pi r^2$ $= 60 \text{ } m \times 100 \text{ } m + 3,14 \times 60^2 \text{ } m^2 \checkmark \checkmark \mathbf{M}$ $= 6\ 000 \text{ } m^2 + 11\ 304 \text{ } m^2$ $= 17\ 304 \text{ } m^2 \checkmark \mathbf{A}$</p>		<p>Formula/ substitution: 2 marks</p> <p>Answer: 1 mark</p>	(3)