



Province of the
EASTERN CAPE
EDUCATION

**NATIONAL SENIOR CERTIFICATE/
*NASIONALE SENIOR SERTIFIKAAT***

GRADE/*GRAAD* 12

JUNE/*JUNIE* 2019

**TECHNICAL MATHEMATICS P2/*TEGNIESE WISKUNDE V2*
MARKING GUIDELINE/*NASIENRIGLYN***

MARKS/*PUNTE*: 150

This marking guideline consists of 16 pages./
Hierdie nasienriglyn bestaan uit 16 bladsye.

NOTE:

- Continuous accuracy (CA) applies in ALL aspects of the marking guideline.
- Assuming values/answers in order to solve a problem is unacceptable.

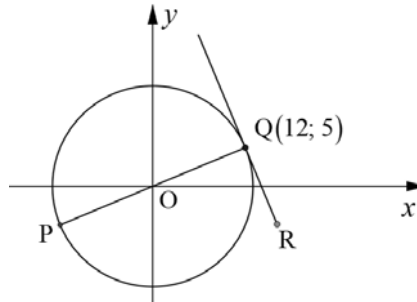
LET WEL:

- *Volgehoue akkuraatheid (CA) is deurgaans in ALLE aspekte van die nasienriglyn van toepassing.*
- *Aanvaarding van waardes/antwoorde om 'n probleem op te los, is onaanvaarbaar.*

MARKING CODES / NASIENKODES	
M	Method/ <i>Metode</i>
MA	Method with accuracy/ <i>Metode met akkuraatheid</i>
A	Accuracy/ <i>Akkuraatheid</i>
CA	Consistent accuracy/ <i>Deurlopende akkuraatheid</i>
S	Simplification/ <i>Vereenvoudiging</i>
SF	Substitution into the correct formula/ <i>Vervanging in die korrekte formule</i>
R	Rounding penalty/ <i>Afronding penalisering</i>
RE	Reason/ <i>Rede</i>
ST	Statement/ <i>Bewering</i>
SR	Statement and correct reason/ <i>Bewering en korrekte rede</i>

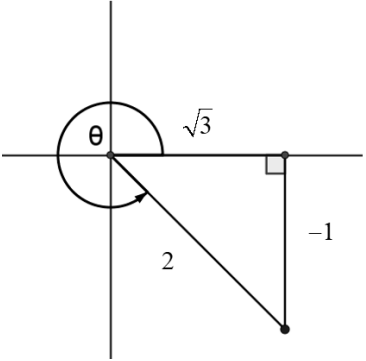
QUESTION/VRAAG 1			
1.1	$AB = \sqrt{(-2 - (-4))^2 + (2 - (-1))^2}$ $= \sqrt{13}$ $= 3,61$	✓ SF/A ✓ CA Answer/Antwoord	(2)
1.2	$m_{AB} = \frac{2 - (-1)}{-2 - (-4)}$ $= \frac{3}{2}$	✓ SF/A ✓ A	(2)
1.3	$m_{CD} = m_{AB} = \frac{3}{2} \quad AB \parallel CD$ $y - y_1 = m(x - x_1)$ $y - 0 = \frac{3}{2}(x - 2)$ $y = \frac{3}{2}x - 3$	✓ ST ✓ SF/CA ✓ CA Equation/Vergelyking	(3)
1.4	$\tan \alpha = \frac{3}{2}$ $\alpha = \tan^{-1}\left(\frac{3}{2}\right)$ $= 56,31^\circ$	✓ M ✓ CA 56,31°	(2)
1.5	$1 = \frac{y_D - 1}{2}$ $y_D - 1 = 2$ $y_D = 3$	✓ M ✓ A	(2)
			[11]

QUESTION/VRAAG 2

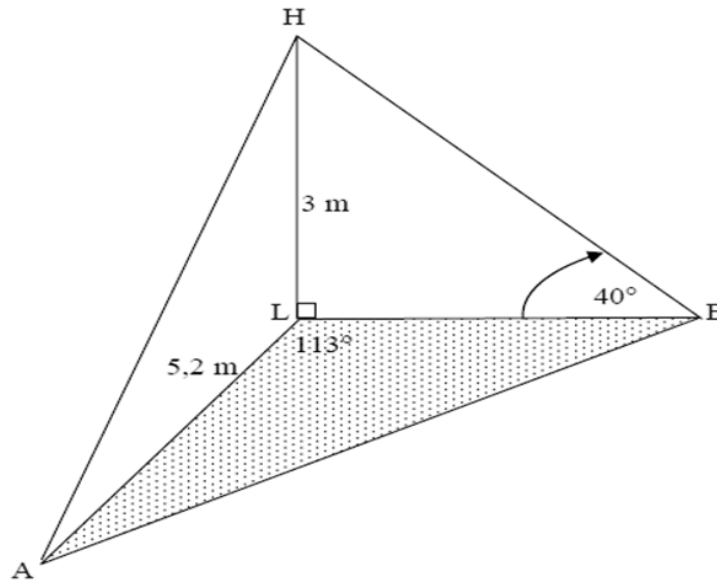


2.1.1	$x^2 + y^2 = r^2$ $(12)^2 + (5)^2 = r^2$ $169 = r^2$ $x^2 + y^2 = 169$	✓SF/A ✓A Equation of circle/vergelýking van sirkel	(2)
2.1.2	$m_{PQ} = \frac{5}{12}$ $m_{RQ} = -\frac{12}{5} \text{ (product of gradients)}$ $y - y_1 = m(x - x_1)$ $y - 5 = -\frac{12}{5}(x - 12)$ $y = -\frac{12}{5}x + \frac{169}{5}$	✓A gradient/gradient PQ ✓CA gradient/gradient RQ ✓SF/A ✓CA equation/vergelýking	(4)
2.2.1	$9x^2 + 16y^2 = 144$ $\frac{x^2}{16} + \frac{y^2}{9} = 1$	✓A LHS/LK ✓A RHS/RK = 1	(2)
2.2.2	Major axis / Groter-as = 8 Minor axis / Kleiner-as = 6	✓CA ✓CA	(2)
2.2.3		✓CA both x-intercepts/beide x-afsnitte ✓CA both y-intercepts/beide y-afsnitte ✓CA elliptical shape/eliptiese vorm	(3)
			[13]

QUESTION/VRAAG 3			
3.1	$\frac{\cos e c^2 100^\circ}{-\sec 80^\circ}$ $= -0,179$	✓✓A R	(2)
3.2.1	$\tan(180^\circ - \theta) \cdot \cos^2(180^\circ + \theta) + \cos(180^\circ - \theta) \cdot \sin \theta \cdot \sec \frac{\pi}{3}$ $= (-\tan \theta)(-\cos \theta)^2 + (-\cos \theta)(\sin \theta)(\sec 60^\circ)$ $= \left(-\frac{\sin \theta}{\cos \theta}\right)(\cos^2 \theta) - \cos \theta \sin \theta (2)$ $= -\sin \theta \cos \theta - 2 \sin \theta \cos \theta$ $= -3 \sin \theta \cos \theta$	✓A (-tan θ) ✓A (-cos θ) ✓A (-cos θ) ✓A 60° ✓A $\frac{\sin \theta}{\cos \theta}$ ✓A (2) ✓CA S	(7)
3.2.2	$\frac{1 - \sin^2 x \cdot \frac{\cos^2 x}{\sin^2 x}}{2(\sin^2 x + \cos^2 x)}$ $= \frac{1 - \cos^2 x}{2(1)}$ $= \frac{\sin^2 x}{2}$	✓A $\frac{\cos x}{\sin x}$ ✓S ✓A $\sin^2 x + \cos^2 x = 1$ ✓CA S	(4)
3.3	$\frac{2}{\sec \theta \sec(360^\circ - \theta) - \tan 45^\circ}$ $= \frac{2}{(\sec \theta) \cdot (\sec \theta) - 1}$ $= \frac{2}{\sec^2 \theta - 1}$ $= \frac{2}{\tan^2 \theta}$ $= 2 \cot^2 \theta$	✓A $\tan 45^\circ = 1$ ✓A (sec θ) ✓A (tan² θ) ✓A $\cot \theta = \frac{1}{\tan \theta}$	(4)
			[17]

QUESTION/VRAAG 4			
4.1.1	 <p> $\sin \theta = \frac{-3}{6}$ $= \frac{-1}{2}$ $x^2 = r^2 - y^2$ $x = \sqrt{2^2 - (-1)^2}$ $= \sqrt{3}$ </p> <p> $\tan \theta = -\frac{1}{\sqrt{3}}$ </p>	<p>✓ A $\sin \theta$ S</p> <p>✓ CA value of x/ waarde van x</p> <p>✓ correct quadrant/ korrekte kwadrant</p>	
4.1.2	$\sin \theta + \sec \theta$ $= \frac{-1}{2} + \frac{2}{\sqrt{3}}$ $= \frac{-\sqrt{3} + 4}{2\sqrt{3}}$	<p>✓ CA $-\frac{1}{2}$</p> <p>✓ CA $\frac{2}{\sqrt{3}}$</p> <p>✓ CA $\frac{-\sqrt{3} + 4}{2\sqrt{3}}$</p>	(4)
4.2	$2\sin \theta - \cos \theta = 0$ $2\sin \theta = \cos \theta$ $\frac{\sin \theta}{\cos \theta} = \frac{1}{2}$ $\tan \theta = \frac{1}{2}$ Ref /verwys $\angle = 26,57^\circ$ $\theta = 26,57^\circ$ or/of $180^\circ + 26,57^\circ = 206,57^\circ$	<p>✓ A $\tan \theta = \frac{1}{2}$</p> <p>✓ CA Ref/verwys \angle</p> <p>✓ CA $\theta = 26,57^\circ$</p> <p>✓ M $180^\circ +$</p> <p>✓ CA $\theta = 206,57^\circ$</p>	(5)
			[12]

QUESTION/VRAAG 5



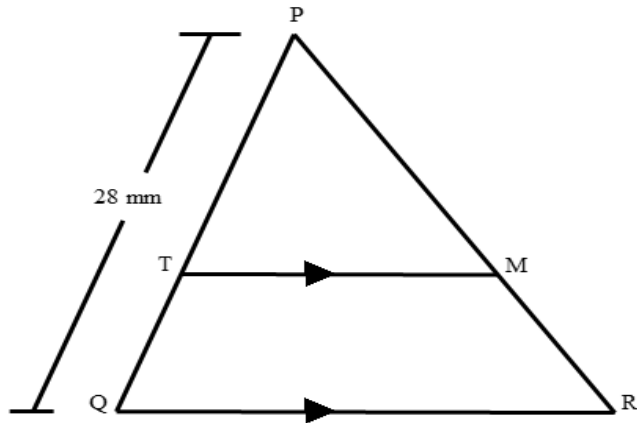
5.1	$\widehat{BHL} = 180^\circ - (90^\circ + 40^\circ)$ $= 50^\circ$	✓A	(1)
5.2	$\text{In } \triangle BHL \quad \cot 40^\circ = \frac{LB}{3}$ $\tan 50^\circ = \frac{LB}{3} \quad \text{OR/OF} \quad LB = 3 \cot 40^\circ$ $LB = 3 \tan 50^\circ \quad = 3,58 \text{ m}$	✓M ✓A	(2)
5.3	$AB^2 = AL^2 + LB^2 - 2 \cdot AL \cdot LB \cdot \cos \widehat{ALB}$ $AB = \sqrt{(5,2)^2 + (3,58)^2 - 2(5,2)(3,58) \cos(113^\circ)}$ $= 7,38 \text{ m}$	✓M ✓A SF ✓CA S	(3)
5.4	$\Delta ALB = \frac{1}{2} AL \times LB \cdot \sin \widehat{ALB}$ $= \frac{1}{2} (5,2)(3,58) \sin(113^\circ)$ $= 8,57 \text{ m}^2$	✓M ✓A SF ✓CA S	(3)
			[9]

QUESTION/VRAAG 6			
6.1	$f(x) = 2 \cos x$ and $g(x) = \sin(x - 30^\circ)$		
		<p>f:</p> <ul style="list-style-type: none"> ✓ x-intercepts / x-afsnitte ✓ Turning points / draaipunte ✓ shape/vorm <p>g:</p> <ul style="list-style-type: none"> ✓ x-intercepts / x-afsnitte ✓ Turning points / draaipunte ✓ shape/vorm 	(6)
6.2	Amplitude $f = 2$	✓ A	(1)
6.3	Period $g = 360^\circ$	✓ A	(1)
6.4	$x \in (0^\circ; 30^\circ]$ or / of $x \in [210^\circ; 360^\circ)$	<ul style="list-style-type: none"> ✓ CA end points/ eindpunte ✓ CA notation/notasie <ul style="list-style-type: none"> ✓ CA end points/ eindpunte ✓ CA notation/notasie 	(4)
			[12]

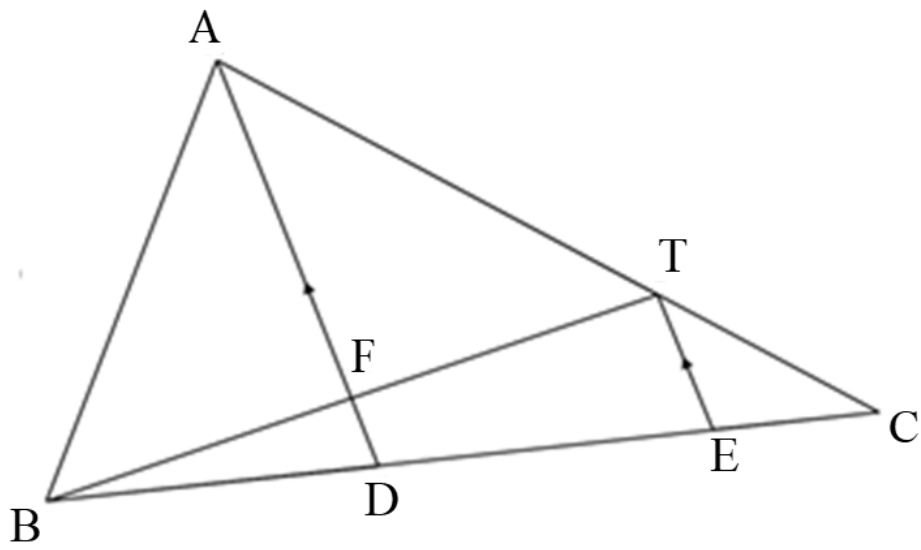
QUESTION/VRAAG 7			
7.1.1	Perpendicular/ <i>loodreg</i>	✓A	(1)
7.1.2	Equal/ <i>gelyk</i>	✓A	(1)
7.1.3	Supplementary/ <i>aanvullend</i>	✓A	(1)
7.2			
7.2.1	Let $DO = x$ cm $\therefore BO = (x + 6)$ cm $\therefore (x + 6)^2 = x^2 + 15^2$ (Pyth) $x^2 + 12x + 36 = x^2 + 225$ $12x = 189$ $x = 15,75$ $DO = 15,75$ cm	✓M Apply Pyth/ <i>Toepassing Pyth</i> ✓ST ✓S ✓CA length of DO/ <i>Lengte van DO</i>	(4)
7.2.2	$\tan \hat{D}OB = \frac{15}{15,75}$ $\hat{D}OB = 43,6^\circ$ $\hat{A}OB = 2\hat{D}OB = 2(43,6^\circ) = 87,2^\circ$	✓M ✓S ✓S	(3)

<p>7.3</p>			
<p>7.3.1</p>	<p>RS is a tangent, because it touches the surface at one point only./RS is 'n raaklyn omdat dit die oppervlakte by slegs een punt raak.</p>	<p>✓A tangent/raaklyn ✓A touches one point/raak by een punt</p>	<p>(2)</p>
<p>7.3.2</p>	<p>$\hat{D}BC = 40^\circ$ tan-chord thm $\hat{C}DB = 40^\circ$ \angle^s opp equal side</p>	<p>✓ST ✓RE ✓SR</p>	<p>(3)</p>
<p>7.3.3</p>	<p>$\hat{D}_3 = 90^\circ - (\hat{D}_2 + \hat{D}_1)$ tan \perp rad $= 10^\circ$ $\hat{B}_2 = 10^\circ$ \angle^s opp equal side; $OB = OD$ (radii)</p>	<p>✓ST ✓RE ✓SR</p>	<p>(3)</p>
<p>7.3.4</p>	<p>$\hat{B}DS = 80^\circ$ $\hat{A} = 80^\circ$ (tan-chord) OR/OF $\hat{C} = 100^\circ$ \angle^s of Δ thm $\hat{A} = 80^\circ$ opp \angle^s of cyclic quad OR/OF $\hat{O}_1 = 160^\circ$ Int \angle^s of Δ $\hat{A} = 80^\circ$ \angle at centre = $2 \times \angle$ at circumf</p>	<p>✓ST ✓ST ✓RE OR/OF ✓SR ✓ST ✓RE OR/OF ✓SR ✓ST ✓RE</p>	<p>(3)</p>
			<p>[21]</p>

QUESTION/VRAAG 8



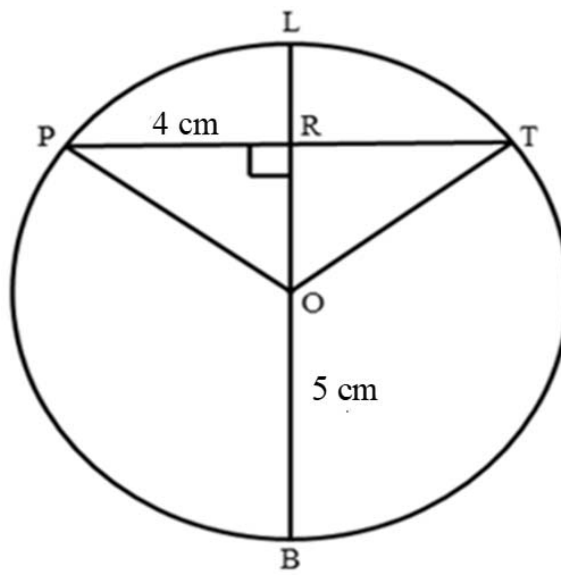
8.1	$\frac{TQ}{PQ} = \frac{MR}{PR}$ <p>prop theorem; $TM \parallel QR$</p> $= \frac{3}{7}$ $TQ = \frac{3}{7} \times 28$ $TQ = 12 \text{ mm}$	<p>✓ST ✓RE</p> <p>✓S</p> <p>✓S</p>	(4)
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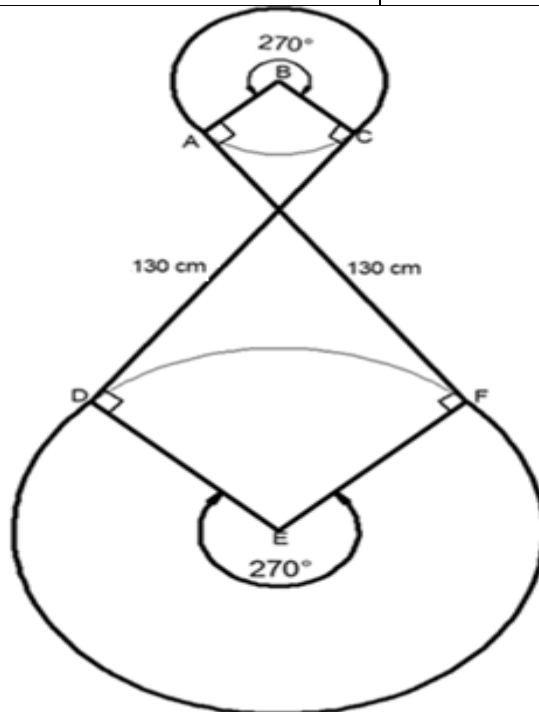
8.2.1	$\frac{CE}{ED} = \frac{1}{2}$ <p>prop theorem; $TE \parallel AD$</p>	<p>✓ST</p> <p>✓RE</p>	(2)
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8.2.2	$\frac{DE}{DC} = \frac{AT}{AC} = \frac{2}{3}$ <p>prop theorem; AD//TE</p> $DE = \frac{2}{3} \times 9$ $= 6$ <p>$\therefore D$ is the mid-pt of BE $BD = DE = 6$</p>	<p>✓SR ✓RE</p> <p>✓S</p> <p>✓S</p>	(4)
8.2.3	<p>BD = DE D as mid-pt BE, proved</p> <p>BF = TF line through midpt \square to 2nd side</p> <p>TE = 2DF Midpt theorem</p> <p>TE = 4 cm</p>	<p>✓ST ✓RE</p> <p>✓SR</p> <p>✓ST</p>	(4)
8.2.4	$\frac{\text{Area } \triangle ADC}{\text{Area } \triangle ADB} = \frac{\frac{1}{2} \times h \times DC}{\frac{1}{2} \times h \times BD}$ <p>DC = 9 BD = 6</p> <p>\triangle^s have same height from A on BC</p> $\therefore \frac{\text{Area } \triangle ADC}{\text{Area } \triangle ABD} = \frac{9}{6}$ $= \frac{3}{2}$	<p>✓M</p> <p>✓S</p> <p>✓S</p>	(3)
			[17]

QUESTION/VRAAG 9



9.1	$4h^2 - 4dh + x^2 = 0$ $4h^2 - 4(10)h + 8^2 = 0$ $4h^2 - 40h + 64 = 0$ $h^2 - 10h + 16 = 0$ $(h - 2)(h - 8) = 0$ $h = 2 \text{ cm} \ \& \ 8 \text{ cm}$	<ul style="list-style-type: none">✓ A formula/formule✓ SF/A✓ S✓ S: factorizing/faktorisering✓ S: heights/hogtes	(5)
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9.2.1	$s = r\theta$ $= 85 \times 270^\circ \times \frac{\pi}{180^\circ}$ $= 127,5\pi$ $\approx 401 \text{ cm}$	✓A formula/formule ✓A SF ✓ $\frac{\pi}{180^\circ}$ M ✓S	(4)
9.2.2	Length of belt/ <i>Lengte van dryfband</i> = $165 + 130 \times 2 + 401 = 826 \text{ cm}$	✓M ✓CA belt length/ <i>bandlengte</i>	(2)
9.3.1	$\omega = 2\pi n$ $= 2\pi \left(\frac{420}{1m} \right) \left(\frac{1m}{60s} \right)$ $= 14\pi \text{ rad/s}$ or/of $= 43,98 \text{ rad/s}$	✓A formula/formule ✓A SF ✓A conversion/ <i>herleiding</i> ✓CA angular velocity / <i>hoeksnelheid</i>	(4)
9.3.2	$v = \omega r$ $= 14\pi \left(\frac{240}{2 \times 1000} \right)$ $= \frac{42}{25} \pi$ $= 5,28 \text{ m/s}$ OR/OF $v = \pi Dn$ $= \pi \left(\frac{240}{1000} \right) \left(\frac{420}{60} \right)$ $= 5,28 \text{ m/s}$	✓A formula/formule ✓A SF ✓A conversion/ <i>herleiding</i> ✓A value/ <i>waarde r</i> ✓CA circum velocity / <i>omtreksnelheid</i>	(5)
			[20]

QUESTION/VRAAG 10			
10.1.1	$l = \sqrt{h^2 + r^2}$	✓A	(1)
10.1.2	$\text{Vol}_{\text{cone}} = \frac{1}{3} \text{Vol}_{\text{cylinder}} \quad \text{or} \quad \text{Vol}_{\text{cylinder}} = 3 \text{Vol}_{\text{cone}}$	✓A	(1)
10.1.3	$\pi r \sqrt{h^2 + r^2} = 2\pi r h$ $\sqrt{h^2 + r^2} = 2h$ $h^2 + r^2 = 4h^2$ $r^2 = 3h^2$	✓ST ✓S	(2)
10.1.4	$V_{\text{cone}} = \frac{1}{3} \pi r^2 h$ $= \frac{1}{3} \pi (3h^2) h$ $= \pi h^3$	✓A SF ✓S	(2)
10.1.5(a)	$\text{Vol}_{\text{cylinder}} - \text{Vol}_{\text{cone}} = 54\pi$ $3(\pi h^3) - \pi h^3 = 54\pi$ $2\pi h^3 = 54\pi$ $h^3 = 27$ $h = \sqrt[3]{27}$ $= 3$	✓M ✓A SF ✓S ✓S	(4)
10.1.5(b)	$r^2 = 3h^2$ $= 3(3)^2$ $= 27$ $r = \sqrt{27}$ $= 3\sqrt{3}$	✓A SF ✓A value of/waarde van r	(2)

10.2.1	$A_T = a \left(\frac{o_1 + o_n}{2} + o_2 + o_3 + o_4 + \dots + o_{n-1} \right)$ $= 110 \left(\frac{430 + 347}{2} + 793 + 1167 + 1475 + \dots + 529 \right)$ $= 110(388,5 + 10244)$ $= 1\,169\,575 \text{ km}^2$ <p>OR/OF</p> $A_T = a(m_1 + m_2 + m_3 + \dots + m_n)$ $= 110 \left(\frac{430 + 793}{2} + \frac{793 + 1167}{2} + \frac{1167 + 1475}{2} + \dots + \frac{529 + 347}{2} \right)$ $= 110(611,5 + 980 + 1321 + 1442 + 1420 + 1398 + 1285 + 1037,5 + 699,5 + 438)$ $= 1\,169\,575 \text{ km}^2$	<p>✓ A formula/formule</p> <p>✓ A SF</p> <p>✓ CA value of / waarde van A_T</p> <p>✓ A formula/formule</p> <p>✓ A SF</p> <p>✓ CA value of/waarde van A_T</p>	(3)
10.2.2	<p>Shaded region = Tot_rect_region - map_region</p> $= (110 \times 10) \times 1475 - 1169575$ $= 452\,925 \text{ km}^2$	<p>✓ A Area total region / Area van totale gebied</p> <p>✓ M</p> <p>✓ CA Area</p>	(3)
			[18]
		TOTAL/TOTAAL:	150