



Province of the  
**EASTERN CAPE**  
EDUCATION

**NATIONAL SENIOR  
CERTIFICATE/*NASIONALE  
SENIOR SERTIFIKAAT***

**GRADE/*GRAAD* 12**

**SEPTEMBER 2021**

**TECHNICAL MATHEMATICS P2/*TEGNIESE WISKUNDE V2*  
MARKING GUIDELINE/*NASIENRIGLYN***

**MARKS/*PUNTE*: 150**

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This marking guideline consists of 15 pages./  
*Hierdie nasienriglyn bestaan uit 15 bladsye.*

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**NOTE:**

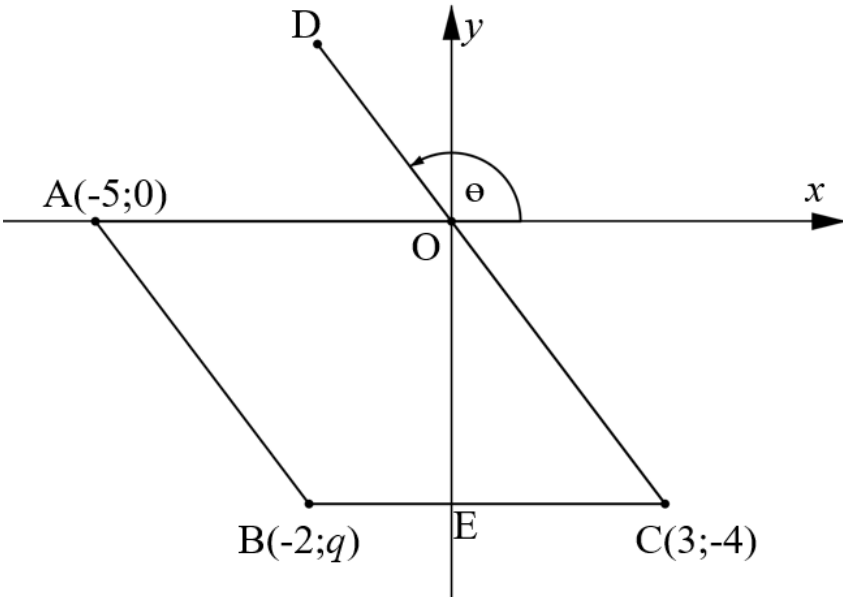
- Continuous accuracy (CA) applies only where indicated in this marking guideline.
- Assuming values/answers in order to solve a problem is unacceptable.

**LET WEL:**

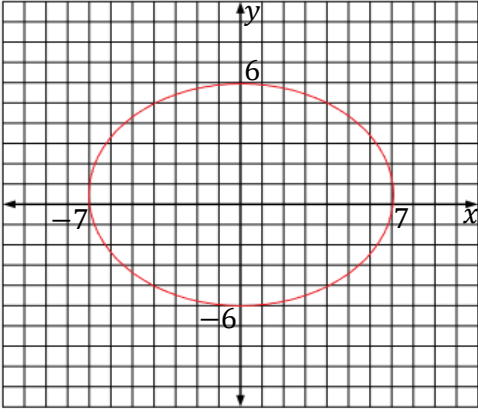
- *Volgehoue akkuraatheid (CA) is slegs van toepassing soos aangedui in hierdie nasienriglyn.*
- *Aanvaarding van waardes/antwoorde om 'n probleem op te los, is onaanvaarbaar.*

<b>MARKING CODES / NASIENKODES</b>	
<b>M</b>	<b>Method / Metode</b>
<b>A</b>	<b>Accuracy / Akkuraatheid</b>
<b>AO</b>	<b>Answer only / Slegs antwoord</b>
<b>CA</b>	<b>Consistent accuracy / Deurlopende akkuraatheid</b>
<b>F</b>	<b>Formula / Formule</b>
<b>I</b>	<b>Identity / Identiteit</b>
<b>R</b>	<b>Rounding / Afronding</b>
<b>S</b>	<b>Simplification / Vereenvoudiging</b>
<b>ST</b>	<b>Statement / Bewering</b>
<b>RE</b>	<b>Reason / Rede</b>
<b>ST RE</b>	<b>Statement and correct reason / Bewering en korrekte rede</b>
<b>SF</b>	<b>Substitution correctly in correct formula / Korrekte vervanging in die korrekte formule</b>
<b>NPU</b>	<b>No penalty for omitting units / Geen penalisering vir eenhede uitgelaat</b>

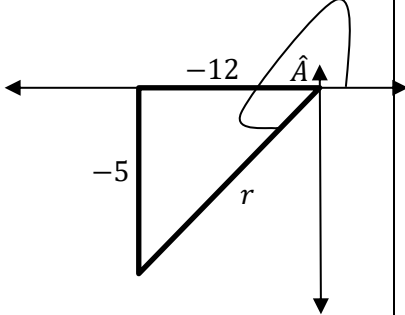
QUESTION/VRAAG 1

Q		M
		
1.1	$q = -4$	✓ A (1)
1.2	$AB^2 = (-2 + 5)^2 + (-4 - 0)^2$ $= 9 + 16$ $AB = 5 \text{ units / eenhede}$	✓ M ✓ 5 CA (2)
1.3	$m_{CD} = \frac{-4-0}{3-0}$ $= -\frac{4}{3}$ $\tan \theta = -\frac{4}{3}$ $\text{Ref / verw} \angle = \tan^{-1} \left( \frac{4}{3} \right)$ $= 53,13^\circ$ $\therefore \theta = 126,87^\circ$	✓ $-\frac{4}{3}$ A  ✓ 53,13° CA ✓ 126,87° CA (3)
1.4	$BC = 3 - (-2) = 3 + 2 = 5 \text{ units / eenhede}$ $AO = 0 - (-5) = 5 \text{ units / eenhede}$ <p><math>\therefore</math> ABCO is a parallelogram (One pair of opp. side = and <math>\parallel</math> / Een paar teenoorstaande sye = en <math>\parallel</math>)</p> <p>But / maar, <math>AO = AB</math> (from / vanuit 1.2)</p> <p><math>\therefore</math> ABCO is a rhombus / is 'n ruit (parallelogram with all sides = / parallelogram met all sye =)</p>	✓ BC & AO M  ✓ parm and / en reason / rede  ✓ rhombus / ruit ✓ reason / rede (4)
		<b>[10]</b>

## QUESTION/VRAAG 2

Q		M	
2.1.1	$x^2 + y^2 = 25 \dots 1$ $y - x - 1 = 0 \dots 2$ $y = x + 1 \dots 3$ sub 3 in 1: $x^2 + (x + 1)^2 = 25$ $x^2 + x^2 + 2x + 1 = 25$ $2x^2 + 2x - 24 = 0$ $x^2 + x - 12 = 0$ $(x + 4)(x - 3) = 0$ $x = -4$ or / of $x = 3$ $\therefore y = -3$ or/of $y = 4$	$\checkmark y = x + 1$ $\checkmark x^2 + (x + 1)^2 = 25$ $\checkmark x^2 + x - 12 = 0$ $\checkmark x = -4$ $\checkmark x = 3$ $\checkmark y = -3$ CA $\checkmark y = 4$ CA (7)	
2.1.2	$(3; 2): (3)^2 + (2)^2 = 13$ $\therefore x^2 + y^2 < r^2$ $\therefore$ lies inside the circle / lê binne die sirkel	$\checkmark 13$ $\checkmark x^2 + y^2 < r^2$ CA $\checkmark$ conclusion / afleiding (3)	
2.1.3	$m_{rad} = \frac{0-3}{0-(-4)}$ $= -\frac{3}{4}$ $\therefore m_{tan} \times m_{rad} = -1$ $\therefore m_{tan} \times -\frac{3}{4} = -1$ $\therefore m_{tan} = -1 \div -\frac{3}{4}$ $\therefore m_{tan} = \frac{4}{3}$ $y = mx + c$ $\therefore y = \frac{4}{3}x + c$ $(-4; 3): 3 = \frac{4}{3}(-4) + c$ $3 = \frac{-16}{3} + c$ $\frac{25}{3} = c$ $\therefore y = \frac{4}{3}x + \frac{25}{3}$	$\checkmark -\frac{3}{4}$ $\checkmark \frac{4}{3}$ $\checkmark \frac{25}{3} = c$ $\checkmark y = \frac{4}{3}x + \frac{25}{3}$ CA (4)	
2.2	$36x^2 + 49y^2 = 1764$ $\frac{36x^2}{1764} + \frac{49y^2}{1764} = 1$ $\frac{x^2}{49} + \frac{y^2}{36} = 1$		$\checkmark \frac{x^2}{49} + \frac{y^2}{36} = 1$ $\checkmark$ Shape / vorm $\checkmark$ x-intercept / x-afsnit $\checkmark$ y-intercept / y-afsnit (4)
		<b>[18]</b>	

QUESTION/VRAAG 3

Q		M
3.1.1	$\tan 4(122.3^\circ) + \frac{2}{3} \cos \left( \frac{210.5^\circ}{4} \right)$ $= -0,8$	✓ SF ✓ -0,8 (2)
3.1.2	$\frac{1}{\sin \left( \frac{\hat{A}}{3} + 2B \right)}$ $= \frac{1}{\sin \left( \frac{210.5^\circ}{3} + 2(122.3^\circ) \right)}$ $= -1,4$	✓ $\frac{1}{\sin \left( \frac{\hat{A}}{3} + 2B \right)}$ ✓ SF ✓ -1,4 (3)
3.2.1	$\tan \hat{A} = \frac{5}{12} = \frac{-5}{-12}$ $\therefore \operatorname{cosec}^2 \hat{A} = \frac{1}{\sin^2 \hat{A}}$ $\operatorname{cosec}^2 \hat{A} = \frac{169}{25}$ <p style="text-align: center;"><b>OR/OF</b></p> $\tan \hat{A} = \frac{5}{12} = \frac{-5}{-12}$ $\therefore \operatorname{cosec}^2 \hat{A} = \left( \frac{13}{-5} \right)^2$ $\operatorname{cosec}^2 \hat{A} = \frac{169}{25}$	 $\tan \hat{A} = \frac{5}{12} = \frac{-5}{-12} \text{ A}$ ✓ correct quadrant / regte kwadrant A ✓ $r = 13 \text{ A}$ ✓ $\frac{1}{\sin^2 \hat{A}}$ or / of $\operatorname{cosec}^2 \hat{A} = \left( \frac{13}{-5} \right)^2 \text{ CA}$ $\sqrt{\frac{169}{25}} \text{ CA}$ (5)
3.2.2	<p style="text-align: center;"><b>OR/OF</b></p> $\sec \hat{A} - \sin \hat{A} = \frac{1}{\cos \hat{A}} - \sin \hat{A}$ $= \frac{1}{\frac{-12}{13}} - \frac{-5}{13}$ $= \frac{13}{-12} - \frac{-5}{13}$ $= \frac{-12}{-109} - \frac{-5}{13}$ $= \frac{-109}{156}$	$\frac{1}{\cos \hat{A}} \text{ or / of } \sqrt{\frac{13}{-12}}$ $\sqrt{\frac{1}{\frac{-12}{13}}}$ $\sqrt{\frac{-109}{156}} \text{ CA}$ (3)
3.2.3	$\tan \hat{A} = \frac{5}{12}$ $\text{ref / verw} \angle = \tan^{-1} \left( \frac{5}{12} \right)$ $= 22,62^\circ$ $\therefore \hat{A} = 180^\circ + 22,62^\circ$ $\hat{A} = 202,62^\circ$	✓ method / metode ✓ $22,62^\circ$ ✓ $202,62^\circ$ (3)
		<b>[16]</b>

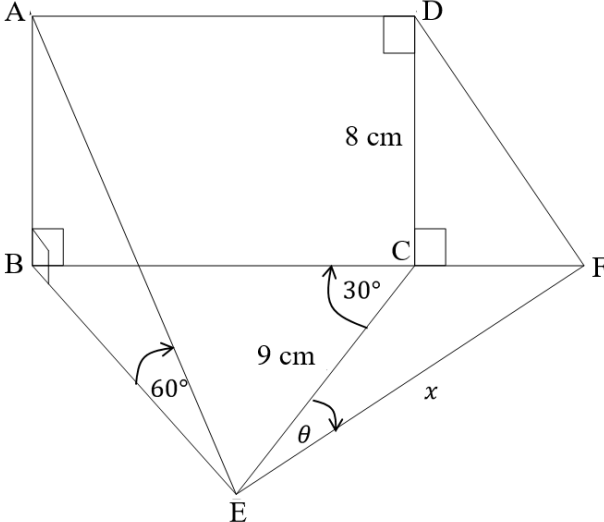
## QUESTION/VRAAG 4

Q		M
4.1	$\frac{\sin(\pi - x) \cdot \operatorname{cosec}(2\pi - x) \cdot \tan(\pi + x)}{\sec(2\pi - x) \cdot \cos(2\pi - x)}$ $= \frac{\sin(180^\circ - x) \cdot \operatorname{cosec}(360^\circ - x) \cdot \tan(180^\circ + x)}{\sec(360^\circ - x) \cdot \cos(360^\circ - x)}$ $= \frac{\sin(x) \cdot -\frac{1}{\sin(x)} \cdot \tan(x)}{\frac{1}{\cos(x)} \cdot \cos(x)}$ $= \frac{-1 \cdot \tan(x)}{1}$ $= -\tan(x)$ <p style="text-align: center;"><b>OR/OF</b></p> $\frac{\sin(\pi - x) \cdot \operatorname{cosec}(2\pi - x) \cdot \tan(\pi + x)}{\sec(2\pi - x) \cdot \cos(2\pi - x)}$ $= \frac{\sin(180^\circ - x) \cdot \operatorname{cosec}(360^\circ - x) \cdot \tan(180^\circ + x)}{\sec(360^\circ - x) \cdot \cos(360^\circ - x)}$ $= \frac{\sin(x) \cdot -\operatorname{cosec}(x) \cdot \tan(x)}{\sec(x) \cdot \cos(x)}$ $= \frac{-1 \cdot \tan(x)}{1}$ $= -\tan(x)$	<p>✓ correct conversion of rad to degrees / korrekte herleiding van rad na grade</p> <p>✓ <math>\sin(x)</math></p> <p>✓ <math>-\frac{1}{\sin(x)}</math></p> <p>✓ <math>\tan(x)</math></p> <p>✓ <math>\frac{1}{\cos(x)}</math></p> <p>✓ <math>\cos(x)</math></p> <p>✓ <math>\frac{-1 \cdot \tan(x)}{1}</math></p> <p>✓ <math>-\tan(x)</math></p> <p style="text-align: right;">(8)</p> <p style="text-align: center;"><b>OR/OF</b></p> <p>✓ correct conversion of rad to degrees / korrekte herleiding van rad na grade</p> <p>✓ <math>\sin(x)</math></p> <p>✓ <math>-\operatorname{cosec}(x)</math></p> <p>✓ <math>\tan(x)</math></p> <p>✓ <math>\sec(x)</math></p> <p>✓ <math>\cos(x)</math></p> <p>✓ <math>\frac{-1 \cdot \tan(x)}{1}</math></p> <p>✓ <math>-\tan(x)</math></p> <p style="text-align: right;">(8)</p>
4.2	$LHS/LK = \frac{\cos\theta}{1-\sin\theta} - \tan\theta$ $= \frac{\cos\theta}{1-\sin\theta} - \frac{\sin\theta}{\cos\theta}$ $= \frac{\cos\theta \cdot \cos\theta - \sin\theta(1-\sin\theta)}{\cos\theta(1-\sin\theta)}$ $= \frac{\cos^2\theta - \sin\theta + \sin^2\theta}{\cos\theta(1-\sin\theta)}$ $= \frac{1 - \sin\theta}{\cos\theta(1-\sin\theta)}$ $= \frac{1}{\cos\theta}$ $= \sec\theta = RHS/RK$	<p>✓ <math>\frac{\sin\theta}{\cos\theta}</math></p> <p>✓ <math>\cos\theta(1 - \sin\theta)</math></p> <p>✓ <math>\cos^2\theta - \sin\theta + \sin^2\theta</math></p> <p>✓ <math>\frac{1-\sin\theta}{\cos\theta(1-\sin\theta)}</math></p> <p>✓ <math>\frac{1}{\cos\theta}</math></p> <p style="text-align: right;">(5)</p>
		<b>[13]</b>

QUESTION/VRAAG 5

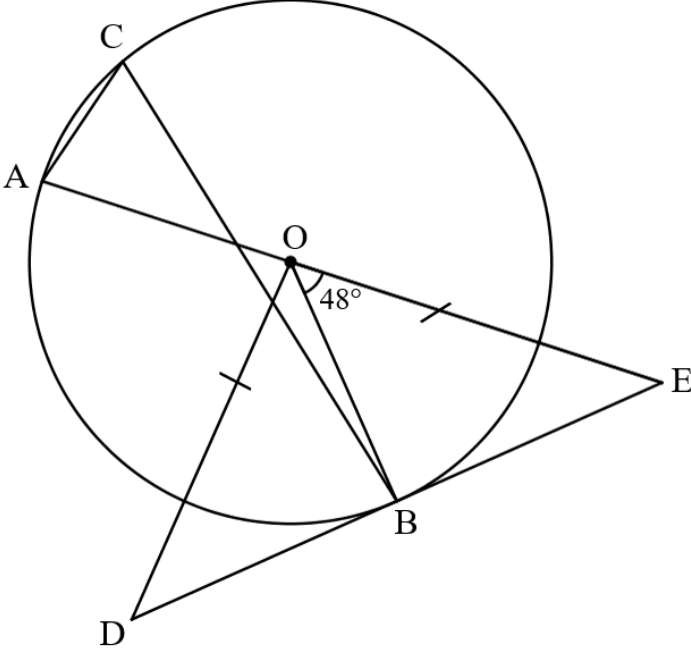
Q			M
5.1			<ul style="list-style-type: none"> <li>✓ cos start and end point / cos begin- en eindpunte</li> <li>✓ cos turningpoints / cos draaipunte</li> <li>✓ cos x-intercepts/cos x-afsnitte</li> <li>✓ sin start and end point / sin begin- en eindpunte</li> <li>✓ sin turningpoints / sin draaipunte</li> <li>✓ sin x-intercepts/sin x-afsnitte</li> </ul> <p style="text-align: right;">(6)</p>
5.2.1	120°		<ul style="list-style-type: none"> <li>✓ 120°</li> </ul> <p style="text-align: right;">(1)</p>
5.2.2	(a)	$x = 30^\circ$ and / en $x = 120^\circ$	<ul style="list-style-type: none"> <li>✓ <math>x = 30^\circ</math></li> <li>✓ <math>x = 120^\circ</math></li> </ul> <p style="text-align: right;">(2)</p>
	(b)	$90^\circ \leq x \leq 150^\circ$	<ul style="list-style-type: none"> <li>✓ <math>90^\circ \leq</math></li> <li>✓ <math>\leq 150^\circ</math></li> </ul> <p style="text-align: right;">(2)</p>
			<b>[11]</b>

## QUESTION/VRAAG 6

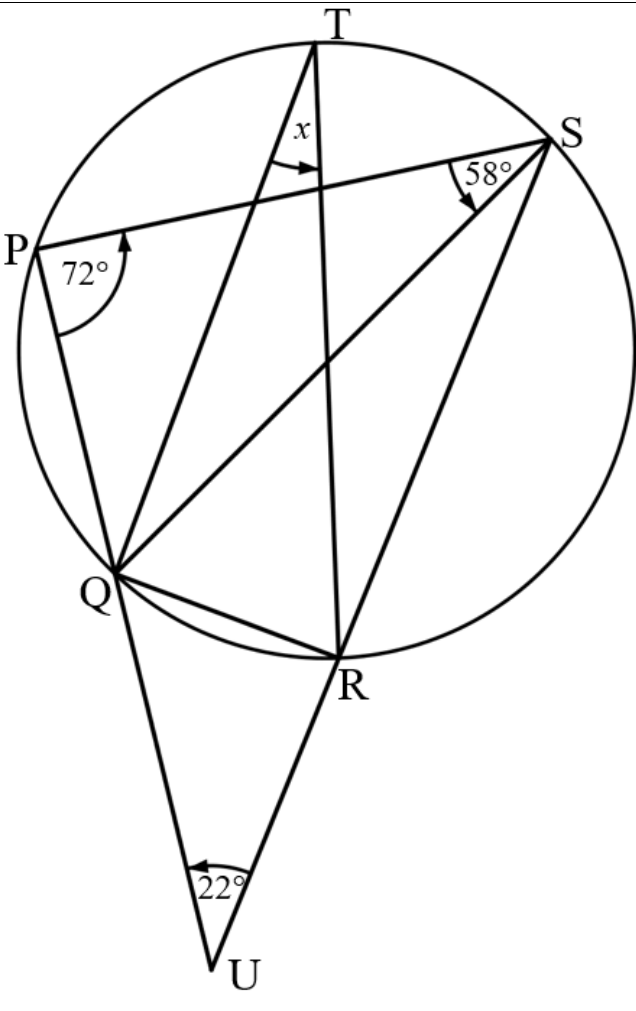
Q		M
		
6.1	$AB = 8 \text{ cm}$ (opp sides of rec = / teenoorst. sye van reghoek =)	✓ 8 cm <b>ST</b> ✓ <b>RE</b> (2)
6.2	$\frac{BE}{8} = \tan 30^\circ$ $BE = 4,62 \text{ cm} = 5 \text{ cm}$	✓ $\frac{BE}{8} = \tan 30^\circ$ <b>M</b> ✓ 5 cm (2)
6.3	$\frac{\sin \widehat{EBC}}{9} = \frac{\sin 30^\circ}{4,62}$ $\sin \widehat{EBC} = \frac{\sin 30^\circ}{4,62} \times 9$ $\widehat{EBC} = 76,91^\circ = 77^\circ$	✓ <b>SF</b> ✓ $\sin \widehat{EBC} = \frac{\sin 30^\circ}{4,62} \times 9$ 9 ✓ $77^\circ$ (3)
6.4	$\widehat{BEC} = 180^\circ - 30^\circ - 77^\circ$ $= 73^\circ$ (Int. $\angle$ 's of $\triangle BEC$ / Binne. $\angle$ 'e van $\triangle BEC$ ) $\text{Area } \triangle BCE = \frac{1}{2} a \cdot b \cdot \sin \widehat{C}$ $= \frac{1}{2} (5)(9) \sin 73^\circ$ $= 21,52 \text{ cm}^2$	✓ <b>ST RE</b> ✓ $\frac{1}{2} (5)(9) \sin 73^\circ$ <b>SF</b> ✓ $21,52 \text{ cm}^2$ <b>CA</b> (3)
6.5	$CF^2 = CE^2 + FE^2 - 2(CE)(FE) \cos \widehat{CEF}$ $CF^2 = (9)^2 + (10)^2 - 2(9)(10) \cos(25^\circ)$ $= 17,86 \dots$ $CF = \sqrt{17,86 \dots}$ $CF = 4,22 \dots = 4 \text{ cm}$	✓ $(9)^2 + (10)^2 - 2(9)(10) \cos(25^\circ)$ <b>SF</b> ✓ $17,86 \dots$ <b>S</b> ✓ 4 cm <b>CA</b> (3)
		<b>[13]</b>



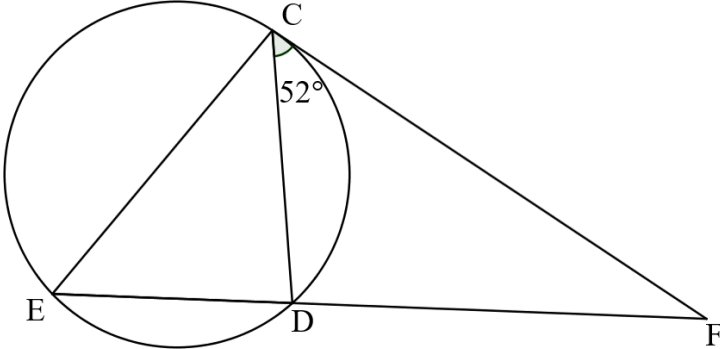
QUESTION/VRAAG 7

Q		M
7.1	double the size of the angle subtended by the same arc at the circumference of a circle / <i>is dubbel die grootte van die hoek wat dit by dieselfde koord die omtrek van 'n sirkel onderspan</i>	✓  (1)
7.2		
7.2.1	$A\hat{O}B = 180^\circ - 48^\circ \dots(\text{suppl. } \angle\text{'s} / \text{suppl. } \angle\text{'e})$ $= 132^\circ$	✓ <b>ST RE</b>  (1)
7.2.2	$\hat{C} = \frac{1}{2}(132^\circ) \dots(\angle \text{ at centre} = 2 \times \angle \text{ at circum.} / \angle \text{ by midpt} = 2 \times \angle \text{ by omtrek})$ $= 66^\circ$	✓ <b>RE</b> ✓ <b>66° ST</b>  (2)
7.2.3	$O\hat{B}E = 90^\circ \dots(\text{tan } \perp \text{ rad})$ $A\hat{E}D = 180^\circ - (90^\circ + 48^\circ)$ $= 42^\circ (\text{int } \angle\text{'s of triangle} / \text{binne } \angle\text{'e van driekhoek})$	✓ <b>ST</b> ✓ <b>RE</b> ✓ <b>ST RE</b>  (3)
7.2.4	$\hat{D} = A\hat{E}D = 42^\circ \dots(\angle\text{'s opp.} = \text{sides} / \angle\text{'e teenoor} = \text{sye})$ $A\hat{O}D = 84 \dots(\text{ext } \angle \text{ of } \Delta / \text{buite } \angle \text{ van } \Delta)$	✓ <b>ST RE</b> ✓ <b>ST RE</b>  (2)
7.2.5	$BE^2 = OE^2 - OB^2 \dots(\text{Pythagoras})$ $= 7^2 - 5^2$ $= 24$ $BE = \sqrt{24} \approx 4,9 \text{ cm}$	✓ <b>M Pythagoras</b> ✓ <b>ST</b> $BE^2 = 24$ ✓ <b>ST</b> $BE = \sqrt{24}$  (3)
		<b>[12]</b>

QUESTION/VRAAG 8

Q		M
8.1	supplementary / <i>supplementêr</i>	✓ (1)
8.2		
8.2.1 (a)	$\widehat{QSR} = \widehat{T} = x$ ( $\angle$ 's subt.chord QR / ( $\angle$ 'e onderspan deur krd QR)	✓ ST ✓ RE (2)
8.2.2 (b)	$\widehat{PQR} = 180^\circ - (58^\circ + x)$ (opp. $\angle$ 's quad/teenoorts. $\angle$ 'e kvh) $= 122^\circ - x$	✓ ST ✓ RE ✓ $122^\circ - x$ ST (3)
8.2.2	$\widehat{U} + \widehat{UQR} + \widehat{URQ} = 180^\circ$ (int. $\angle$ 's $\Delta$ /binne $\angle$ 'e $\Delta$ ) $22^\circ + 72^\circ + x + 58^\circ = 180^\circ$ $x = 28^\circ$  <b>OR/OF</b> $\widehat{P} + \widehat{S} + \widehat{U} = 180^\circ$ (int. $\angle$ 's $\Delta$ / binne $\angle$ 'e $\Delta$ ) $72^\circ + 58^\circ + x + 22^\circ = 180^\circ$ $x = 28^\circ$	✓ ST RE  ✓ $x = 28^\circ$ ST (2)  <b>OR/OF</b> ✓ ST RE  ✓ $x = 28^\circ$ ST (2)
		[8]

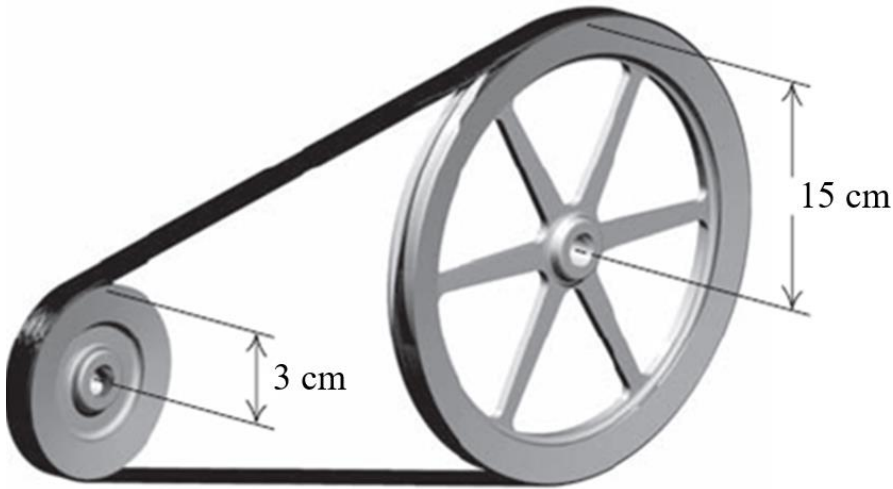
QUESTION/VRAAG 9

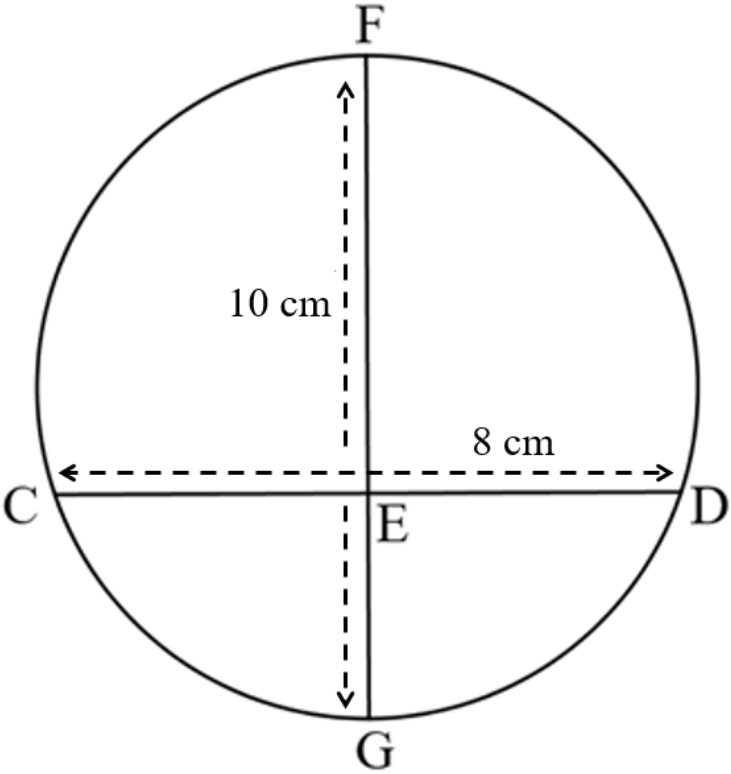
Q		M
9.1	All angles of the one triangle is equal to the angles in the other triangle / <i>Alle hoeke van die een driehoek is gelyk aan die hoeke van die ander driehoek</i> Sides of triangles are in proportion / <i>Sye van die driehoek is in verhouding</i>	✓ ST ✓ ST (2)
9.2		
9.2.1	In $\triangle CDF$ and/en $\triangle ECF$ : $\widehat{FCD} = \widehat{CED} = 52^\circ$ (tanchord / <i>raaklyn koord</i> ) $\widehat{CFD} = \widehat{CFE}$ (common $\angle$ / <i>gemene <math>\angle</math></i> ) $\widehat{CDF} = \widehat{CEC}$ (int. $\angle$ 's $\Delta$ / <i>binne <math>\angle</math>'e <math>\Delta</math></i> ) $\therefore \triangle CDF \parallel \triangle ECF$ ( $\angle\angle\angle$ )	✓ ST RE ✓ ST RE ✓ ST $\triangle CDF \parallel \triangle ECF$ OR ✓ RE ( $\angle\angle\angle$ ) (4)
9.2.2	$\frac{CD}{EC} = \frac{DF}{CF} = \frac{CF}{EF}$ ( $\triangle CDF \parallel \triangle ECF$ ) $\therefore CF^2 = EF \cdot FD$	✓ $\frac{CD}{EC} = \frac{DF}{CF} = \frac{CF}{EF}$ ST ✓ $CF^2 = EF \cdot FD$ ST (2)
9.2.3	$DF = 15 - 6 = 9$ $\frac{CD}{EC} = \frac{DF}{CF} = \frac{CF}{EF}$ (from 9.2.2 / <i>vanuit 9.2.2</i> ) $\therefore \frac{9}{CF} = \frac{CF}{15}$ $\therefore CF^2 = 135$ $\therefore CF \approx 12 \text{ cm}$ <p style="text-align: center;"><b>OR/OF</b></p> $CF^2 = 15 \times 9$ (from 9.2.2 / <i>vanuit 9.2.2</i> ) $CF = \sqrt{135}$ $CF = 11,619 \dots$ $\therefore CF = 12 \text{ cm}$	✓ $DF = 9 \text{ A}$ ✓ $\frac{9}{CF} = \frac{CF}{15}$ SF ✓ $CF^2 = 135 \text{ CA}$ ✓ $12 \text{ cm CA R}$ <p style="text-align: center;"><b>OR/OF</b></p> ✓ $CF^2 = 15 \times 9 \text{ A}$ ✓ $CF = \sqrt{135} \text{ S}$ ✓ $CF = 11,619 \dots \text{ CA}$ ✓ $12 \text{ cm CA R}$ (4)
9.2.4	$\frac{CD}{EC} = \frac{12}{15} = \frac{4}{5}$	✓ $\frac{12}{15}$ SF A ✓ $\frac{4}{5}$ A (2)
9.2.5	$\widehat{ECF} = 44^\circ + 52^\circ = 96^\circ \neq 90^\circ$ $\therefore CE$ not a diameter / <i>CE nie 'n middellyn nie</i> (Diameter not perpendicular to tangent/ <i>middellyn nie loodreg met raaklyn nie</i> )	✓ ST ✓ ST RE (2)

	<b>OR/OF</b>	<b>OR/OF</b>
	$C\hat{D}E = 180^\circ - 44^\circ - 52^\circ = 86^\circ \neq 90^\circ$ $\therefore CE$ not a diameter / $CE$ nie 'n middellyn nie (not Converse $\angle$ 's in semi-circle / nie-omgekeerde $\angle$ 'e in semi-sirkel)	$\checkmark$ ST $\checkmark$ ST RE (2)
		<b>[16]</b>

**QUESTION/VRAAG 10**

<b>Q</b>		<b>M</b>
10.1		
10.1.1	$\hat{A} = 30^\circ \times \frac{\pi}{180^\circ}$ $\hat{A} = \frac{\pi}{6}$ radians / radiale	$\checkmark \times \frac{\pi}{180^\circ}$ $\checkmark$ $\frac{\pi}{6}$ radians/radiale (2)
10.1.2	$s = r\theta$ $BG = (4) \left(\frac{\pi}{6}\right)$ $BG = \frac{2\pi}{3}$ cm	$\checkmark$ F $\checkmark$ SF $\checkmark \frac{2\pi}{3}$ cm (3)
10.1.3	Area of a sector / Opp van 'n sektor = $\frac{r^2\theta}{2}$ $\therefore$ Area of sector AEC / Opp van sektor AEC = $\frac{(5)^2\frac{\pi}{6}}{2}$ $= \frac{3\pi}{2}$ cm <sup>2</sup>	$\checkmark$ F $\checkmark$ SF $\checkmark \frac{3\pi}{2}$ cm <sup>2</sup> (3)
10.1.4	Area of a sector / Opp van 'n sektor = $\frac{r^2\theta}{2}$ $\therefore$ Area of sector ABG / Opp van sektor ABG = $\frac{(4)^2\frac{\pi}{6}}{2}$ $= \frac{4\pi}{3}$ cm <sup>2</sup> $\therefore$ Area of BECG / Opp van BECG = $\frac{27\pi}{4} - \frac{4\pi}{3}$ $\therefore$ Area of BECG / Opp van BECG = $\frac{65\pi}{12}$ cm <sup>2</sup>	$\checkmark$ SF $\checkmark \frac{4\pi}{3}$ $\checkmark$ M $\checkmark \frac{65\pi}{12}$ (4)

<p>10.2</p>		
<p>10.2.1</p>	$\omega = 2\pi n$ $\omega = 2\pi(120)$ $\omega = 240\pi \text{ rad/min}$	<p>✓ <b>F</b>                  ✓ <b>SF</b>                  ✓ <math>240\pi \text{ rad/min}</math>                  (3)</p>
<p>10.2.2</p>	$v = \pi Dn$ $v = \pi(3 \times 2)(120)$ $v = 720\pi \text{ cm/min}$ <p style="text-align: center;"><b>OR/OF</b></p> $v = r\omega$ $v = (3)(240\pi)$ $v = 720\pi \text{ cm/min}$	<p>✓ <b>F</b>                  ✓ <b>SF</b>                  ✓ <math>720\pi \text{ cm/min}</math></p> <p style="text-align: center;"><b>OR/OF</b></p> <p>✓ <b>F</b>                  ✓ <b>SF</b>                  ✓ <math>720\pi \text{ cm/min}</math>                  (3)</p>
<p>10.2.3</p>	<p>Linear speed of large pulley / <i>reglynige spoed van groter katrol</i> =  <math>720\pi \text{ cm / min}</math>  <math>v = \omega r</math>  <math>720\pi = \omega(15)</math>  <math>48\pi \text{ rad / min} = \omega</math></p>	<p>✓ <b>F</b>                  ✓ <b>SF</b>                  ✓ <math>48\pi \text{ rad/min}</math>                  (3)</p>

10.3		
	$4h^2 - 4dh + x^2 = 0$ $4h^2 - 4(10)h + (8)^2 = 0$ $4h^2 - 40h + 64 = 0$ $h^2 - 10h + 16 = 0$ $(h - 8)(h - 2) = 0$ $\therefore h = 8 \text{ cm or/of } h = 2 \text{ cm}$ $\therefore h = 2 \text{ cm}$ <p style="text-align: center;"><b>OR/OF</b></p> <p><math>CE = 4</math> (line from centre perpendicular to chord / lyn vanaf middelpunt loodreg op koord)</p> <p><math>FO = OG</math> (radii)</p> <p><math>OC^2 = OE^2 + CE^2</math> (Pyth)</p> $\therefore OE^2 = OC^2 - CE^2$ $\therefore OE^2 = (5)^2 - (4)^2$ $\therefore OE^2 = 25 - 16$ $\therefore OE^2 = 9$ $\therefore OE = \pm\sqrt{9}$ $\therefore OE = \pm 3$ $\therefore OE = 3 \text{ cm}$ $\therefore EG = 5 - 3$ $\therefore EG = 2 \text{ cm}$	<p>✓ <b>F</b></p> <p>✓ <b>SF</b></p> <p>✓ Standard form/standaard vorm</p> <p>✓ <b>M</b></p> <p>✓ <math>h = 2 \text{ cm}</math></p> <p style="text-align: center;"><b>OR/OF</b></p> <p>✓ <b>ST RE</b></p> <p>✓ <b>ST RE</b></p> <p>✓ <math>OE^2 = (5)^2 - (4)^2</math> <b>SF</b></p> <p>✓ <math>OE = 3 \text{ cm}</math> <b>CA</b></p> <p>✓ <math>EG = 2 \text{ cm}</math> <b>CA</b></p> <p style="text-align: right;">(5)</p>
		<b>[26]</b>

QUESTION/VRAAG 11

Q		M
11.1		
	$A_T = a(m_1 + m_2 + m_3 + \dots + m_n)$ $A_T = 3(6,4 + 5,45 + 4,7 + 4,25 + 4,25)$ $A_T = 3(25,05)$ $A_T = 75,15 \text{ cm}^2$ <p style="text-align: center;"><b>OR/OF</b></p> $A_T = a\left(\frac{o_1 + o_n}{2} + o_2 + o_3 + o_4 + \dots + o_{n-1}\right)$ $A_T = 3\left(\frac{5,9 + 5,4}{2} + 6,9 + 4 + 5,4 + 3,1\right)$ $A_T = 3(25,05)$ $A_T = 75,15 \text{ cm}^2$	<p>✓ F                  ✓ SF                  ✓ S                  ✓ 75,15 cm<sup>2</sup></p> <p style="text-align: center;"><b>OR/OF</b></p> <p>✓ F                  ✓ SF                  ✓ S                  ✓ 75,15 cm<sup>2</sup></p> <p style="text-align: right;">(4)</p>
11.2		
	$TSA = 2\pi r^2 + 2\pi r h - \pi r^2 - \pi r^2$ $TSA = 2\pi \left(\frac{1,85}{2}\right)^2 + 2\pi \left(\frac{1,85}{2}\right) (2,5) - \pi \left(\frac{1,85}{2}\right)^2 - \pi \left(\frac{1}{2}\right)^2$ $TSA = 16,43 \text{ m}^2$	<p>✓ F                  ✓ SF                  ✓ 17,22 m<sup>2</sup></p> <p style="text-align: right;">(3)</p>
		[7]
	<b>TOTAL/TOTAAL:</b>	<b>150</b>